

- MARS M. YAMALEEV, *Splitting properties in 2-c.e. degrees.*

Department of Mathematics, Kazan State University, 18 Kremlyovskaya St., Russia.

*E-mail:* marsiam2@yandex.ru.

A Turing degree  $\mathbf{a}$  is splittable in a class of degrees  $\mathcal{C}$  avoiding an upper cone of a degree  $\mathbf{d}$  if there exist degrees  $\mathbf{x}_0, \mathbf{x}_1 \in \mathcal{C}$  such that  $\mathbf{a} = \mathbf{x}_0 \cup \mathbf{x}_1$ ,  $\mathbf{x}_i < \mathbf{a}$  and  $\mathbf{d} \not\leq \mathbf{x}_i$  for  $i = 0, 1$ . The following theorem presents sufficient conditions for a properly 2-computably enumerable (2-c.e.) degree to be splittable in  $\mathbf{D}_2$  avoiding the upper cone of another properly 2-c.e. degree.

**Theorem 1.** *Let  $\mathbf{a}$  and  $\mathbf{d}$  be properly 2-c.e. degrees such that  $\mathbf{0} < \mathbf{d} < \mathbf{a}$  and there are no c.e. degrees between  $\mathbf{a}$  and  $\mathbf{d}$ . Then the degree  $\mathbf{a}$  is splittable in  $\mathbf{D}_2$  avoiding the upper cone of  $\mathbf{d}$ .*

Theorem 1 holds when  $\mathbf{d}$  is a  $\Delta_2^0$ -degree, which does not contain c.e. sets. Theorem 2 states that the well-known bubble (see [1]) can be constructed in low 2-c.e. degrees.

**Theorem 2.** *There exist low noncomputable 2-c.e. degrees  $\mathbf{b} < \mathbf{a}$  such that for any 2-c.e. degree  $\mathbf{v} \leq \mathbf{a}$  either  $\mathbf{v} \leq \mathbf{b}$  or  $\mathbf{b} \leq \mathbf{v}$ .*

As a consequence we obtain the following: the partial orders of  $m$ -low c.e. and  $m$ -low 2-c.e. degrees are not elementarily equivalent for any  $m \geq 1$ . Also, I will talk about a link between splitting properties (Theorem 1) and the bubbles and how the link could be uniformly adapted to higher levels of the Ershov's hierarchy.

[1] ARSLANOV M.M., KALIMULLIN I.SH., LEMPP S., *On Downey's conjecture.*, **The Journal of Symbolic Logic**, to appear. (<http://www.math.wisc.edu/~lempp/papers>)