▸ ALEXEY. G. VLADIMIROV, *Effectivity properties of intuitionistic set theory with scheme collection.*
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Let $\mathbb{ZFI}2C$ is a intuitionistic two-sorted set theory with variables of sort 0 are variables on natural numbers, and variables of sort 1 are set variables.

Axioms of $\mathbb{ZFI}2C$ consist of usual axioms and schemata of Heyting predicate calculus (HPC), all usual axioms of Heyting Arithmetic (HA), and all usual Zermelo-Fraenkel axioms for set theory including Exstensionality, Collection as Substitution axiom, and transfinite induction as Foundation axiom.

We consider also the additional principle DSC (Double Complement of Sets).

We use some modifications of formalized realizabilities from [1] and proved the following (for T is either $\mathbb{ZFI}2C$ or $\mathbb{ZFI}2C + DCS$):

1. For T : Disjunction Property(DP); Numerical Existensional Property (EP_ω); Curch Rule (CR); Markov Rule (MR); Uniformization Rule (UR).

All these properties are proved with set parameters.

Each combination of the following extra axioms can be added to T with preserving of results (i)-(iii) and (v): Church Thesis CT , Markov Principle M, Uniformization Principle UP, and Independence of Permisses IP.

2. For $T + ECT$ (where ECT is a Extended Church Thesis): Disjunction Property (DP) and EP_ω; the conservativity of $T + ECT$ over T w.r.t. class of all negative formulas; $T + ECT = T + \{R\varphi \equiv \varphi \mid \varphi \text{ is a formula of } T\}$ for a variant of Kleene realizability R.

3. For $T + ECT + M$: the conservativity of $T + ECT + M \vdash \varphi$ over T w.r.t. class of all negative formulas; relative consistency of T w.r.t. $T + ECT + M$); DP and EP_ω for $T + ECT + M$.

4. For $T + nCT + P$: the conservativity of $T + nCT + P \vdash \varphi$ over T w.r.t. class of all negative formulas; relative consistency of $T + nCT + P$ over T; DP and EP_ω for $T + nCT + P$.

[1] M.Beeson, *Continuity in intuitionistic set theories*, ***Logic Collo- quium78.*** North-Holland Publishing Company, 1979, pp. 1–52.